

P. S. SCIENCE & H. D. PATEL ARTS COLLEGE, KADI

Internal Examination

B. Sc. Semester - III

22-9-2016]

C. C. Mathematics - 301

[2 Hours

Calculus and Linear Algebra

1. [A] If function $z = f(x, y)$, defined on an open set $E \subset \mathbb{R}^2$, is differentiable point $(x, y) \in E$, then its partial derivatives f_x and f_y exists at point (x, y) .

[B] Attempt any two

(i) For $f(x, y) = \frac{x^2 + y^2}{x + y}$, $x + y \neq 0$
 0 , $x + y = 0$

determine the value of $xf_x + yf_y$.

- (ii) If $H = f(y - z, z - x, x - y)$ then Prove that

$$H_x + H_y + H_z = 0$$

- (iii) If $u = x \log y + y \log x$ then prove that $u_{xy} = u_{yx}$.

2. [A] If f is a differentiable homogeneous function of x and y of degree m then prove that $xf_x + yf_y = mf(x, y)$

[B] Attempt any two

(i) if $u = \tan^{-1} \left(\frac{x^3 + y^3}{x - y} \right)$ then Prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u$

- (ii) Find the Taylor's expansion of $e^{ax} \cos by$ about

$(0, 0)$ upto and including the terms of 2nd degree.

(1)

[P.T.O.]

(iii) Discuss the extreme value of the function

$$f(x, y) = x^2y^2(1 - x - y)$$

3. [A] Define vector Space with illustration.

[B] Attempt any two

(i) Check the following subsets of \mathbb{R}^3 is Subspace or not ?

$$u = \{(a, a_2, a_3) / a_1 - 2a_2 + a_3 = 0\}$$

(ii) If $e_1 = (3, 2, 1)$, $e_2 = (2, 1, 0)$, $e_3 = (1, 0, 0)$ be three vectors in \mathbb{IR}^3 , then express the vector $(3, 5, 2) \in \mathbb{IR}^3$ as a linear combination of e_1, e_2, e_3

(iii) Show that the vector $(1, 2, 3)$ belongs to

$$[\{(2, 1, 0), (3, 0, -1), (-2, 5, 0)\}]$$
