

P.S.SCIENCE & H.D.PATEL ARTS COLLEGE, KADI
INTERNAL EXAMINATION

08/03/2018 B.Sc. Sem -VI Marks 40
 Number Theory Time: 1.45 to 3.45
 CC-MAT-603 (B)

1. (A) State and Prove Division algorithm

OR

Let a and b are integers, not both zero then $\gcd(a, b) = 1$ iff there exist integers x and y such that, $ax + by = 1$

- (B) Attempt any two:

1. Prove that, a and b are both odd integers then

$$16 \mid a^4 + b^4 - 2$$

2. Find the lcm of 1769 and 2378

3. Solve: $172x + 20y = 1000$

2. (A) For arbitrary integers a and b , $a \equiv b \pmod{n}$ iff a and b leave the same non negative remainders when divided by n

OR

The linear congruence $ax \equiv b \pmod{n}$ has a solution

iff $d \mid b$, where $d = \gcd(a, n)$

- (B) Attempt any two:

1. Solve: $17x \equiv 9 \pmod{276}$

2. Find the remainder when 4444^{4444} divided by 9.

3. Prove that, $7 \mid 2222^{5555} + 5555^{2222}$.

3. (A) State and prove Fermat's theorem.

OR

State and prove Wilson's theorem.

(B) Attempt any two:

1. Prove that, if p and $p+2$ are pair of twin primes then,

$$4((p-1)! + 1) + p \equiv 0 \pmod{p(p+2)}$$

2. Prove that,

$$(p-1)! \equiv p-1 \pmod{1+2+3+\dots+(p-1)}$$

3. Find the last two digits of 9^{9^9} .
