

P.S.SCIENCE & H.D.PATEL ARTS COLLEGE, KADI
INTERNAL EXAMINATION

06/03/2018

B.Sc. Sem -IV
Mathematics
CC-MATH- 401

Marks 40
Time: 1.45 to 3.45

1. (A) Attempt any one.

(i) Obtain the formula for radius of curvature of the curve

$$r = f(\theta).$$

(ii) Prove the relation $\beta(m, n) = \frac{\sqrt{m} \sqrt{n}}{\sqrt{m+n}}$.

(B) Attempt any two.

(i) Find the radius of curvature of the curve

$$r = a(1 - \cos \theta)$$

(ii) Evaluate $\int_0^1 \sqrt{x} \sqrt[3]{1-x^2} dx$ and $\int_{-\infty}^{\infty} e^{-a^2 x^2} dx$

(iii) Find the radius of curvature of the curve

$$x^{2/3} + y^{2/3} = a^{2/3}$$

2. (A) Attempt any one.

(i) Change the order of integration $\int_0^3 \int_{4y/3}^{\sqrt{25-y^2}} f(x, y) dy dx$.

(ii) Evaluate $\int_0^a \int_0^{\sqrt{a^2-x^2}} (x^2 + y^2) dx dy$ by transforming into polar co-ordinate.

(B) Attempt any two.

(i) Find the volume of $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$.

(ii) Find $\iint (x^2 + y^2) dx dy$ over the region bounded by

$$x = 1, x = 2, y = 1, y = x^2$$

(iii) $\iiint_V x^2 dx dy dz$, where V is enclosed by the planes

$$x = 0, y = 0, z = 0 \text{ and } x + y + z = a$$

3. (A) Attempt any one

(i) Prove that

$$\operatorname{div}(\phi f) = \phi \operatorname{div} f + f \cdot (\operatorname{grad} \phi)$$

(ii) State and prove Green's Theorem.

(B) Attempt any two.

(i) Verify Green's theorem

$$\oint_c (3x^2 - 8y^2) dx + (4y - 6xy) dy, \text{ where } c \text{ is the boundary of region bounded by } y^2 = x \text{ and } x^2 = y.$$

(ii) If $f = (2yz, -x^2y, xz^2)$ and $\phi(x, y, z) = 2x^2yz^3$ then

$$(f \cdot \nabla) \phi = f \cdot (\nabla \phi).$$

(iii) Evaluate $\iint_s f \cdot n ds$, where $f = (x + y^2, -2x, 2yz)$ and

surface s is the plane $2x + y + 2z = 6$ in the first octant.